2.5 — Short Run Profit Maximization ECON 306 • Microeconomic Analysis • Fall 2021 Ryan Safner Assistant Professor of Economics ✓ safner@hood.edu

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## Outline

#### **Revenues**

<u>Profits</u>

**Comparative Statics** 

**Calculating Profit** 

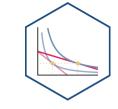
**Short-Run Shut-Down Decisions** 

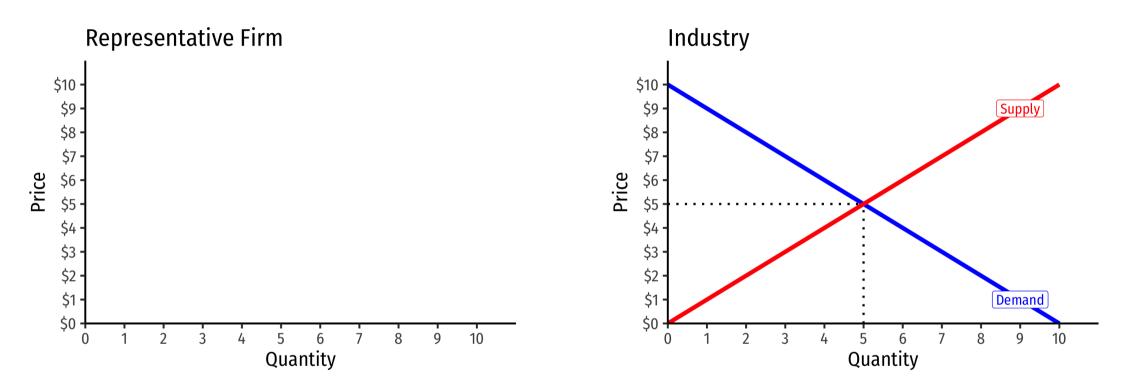
The Firm's Short-Run Supply Decision



#### Revenues

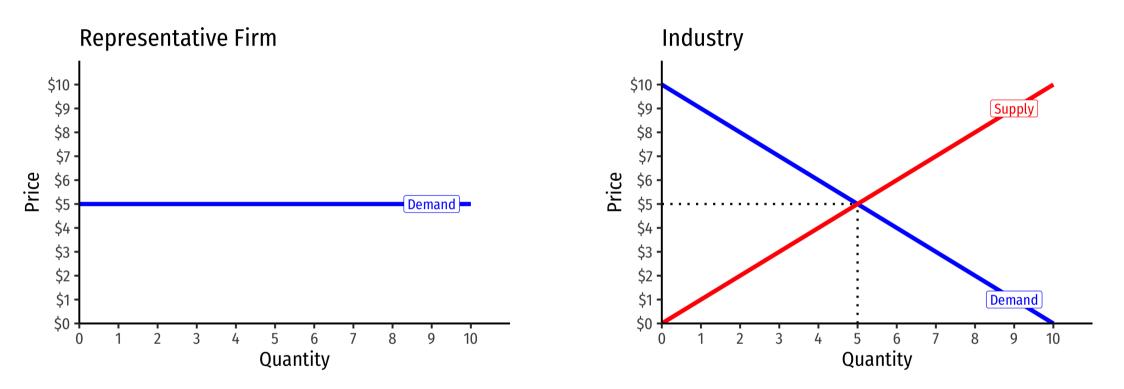
#### **Revenues for Firms in** *Competitive* **Industries I**





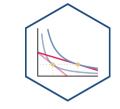
#### **Revenues for Firms in** *Competitive* **Industries I**

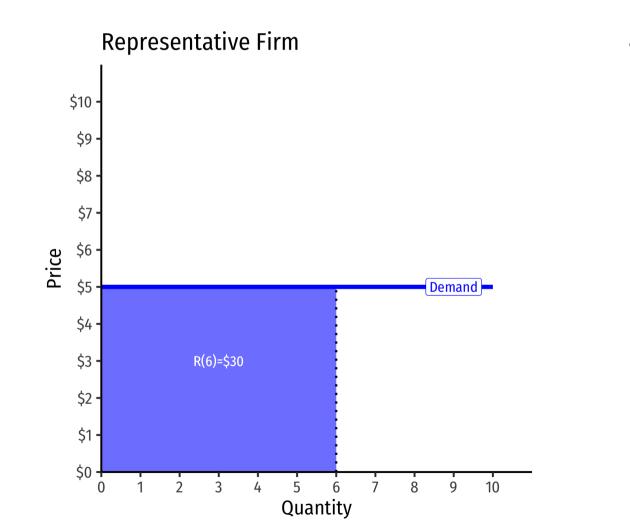




- Demand for a firm's product is **perfectly elastic** at the market price
- Where did the supply curve come from? You'll see

#### **Revenues for Firms in Competitive Industries II**





• Total Revenue R(q) = pq

#### **Average and Marginal Revenues**

• Average Revenue: revenue per unit of output

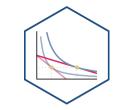
$$AR(q) = \frac{R}{q}$$

• AR(q) is **always** equal to the price! Why?

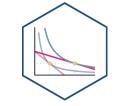
• Marginal Revenue: change in revenues for each additional unit of output sold:

$$MR(q) = \frac{\Delta R(q)}{\Delta q} \approx \frac{R_2 - R_1}{q_2 - q_1}$$

- Calculus: first derivative of the revenues function
- For a <u>competitive</u> firm (only), MR(q) = p, the price!



#### **Average and Marginal Revenues: Example**



**Example**: A firm sells bushels of wheat in a very competitive market. The current market price is \$10/bushel.

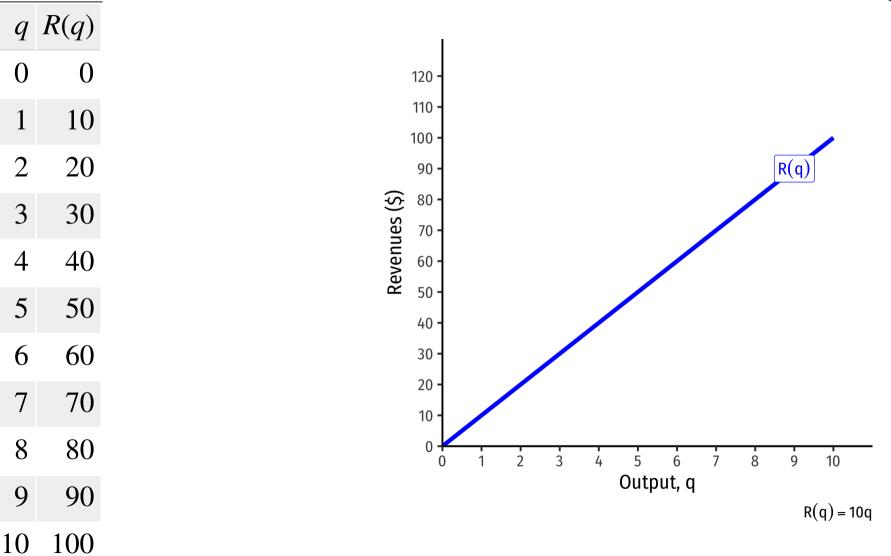
For the 1<sup>st</sup> bushel sold:

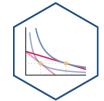
- What is the total revenue?
- What is the average revenue?

For the 2<sup>nd</sup> bushel sold:

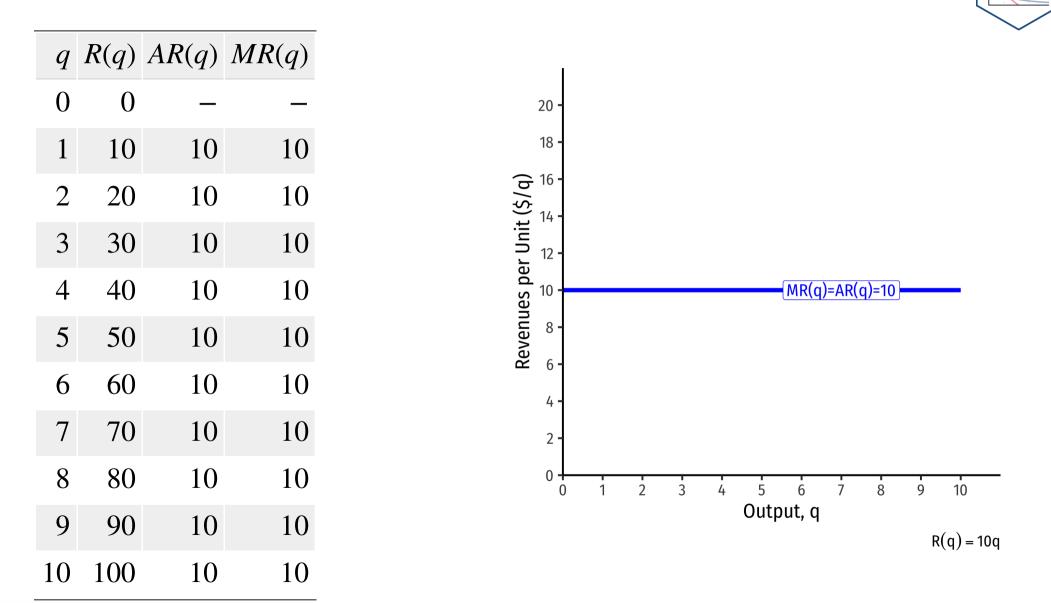
- What is the total revenue?
- What is the average revenue?
- What is the marginal revenue?

#### **Total Revenue, Example: Visualized**





#### **Average and Marginal Revenue, Example: Visualized**



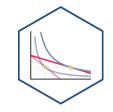


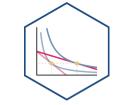
### **Profits**

#### **Recall: The Firm's Two Problems**

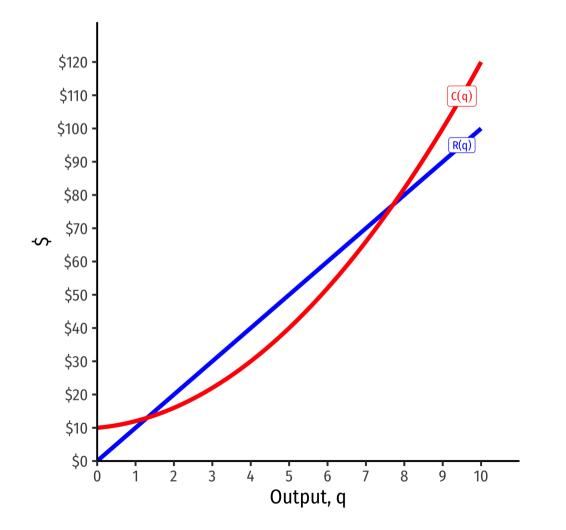
- 1<sup>st</sup> Stage: firm's profit maximization problem:
  - 1. Choose: < output >
  - 2. In order to maximize: < profits >
- 2<sup>nd</sup> Stage: firm's cost minimization problem:
  - 1. Choose: < inputs >
  - 2. In order to *minimize*: < cost >
  - 3. Subject to: < producing the optimal output >
  - Minimizing costs  $\iff$  maximizing profits

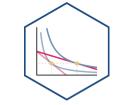




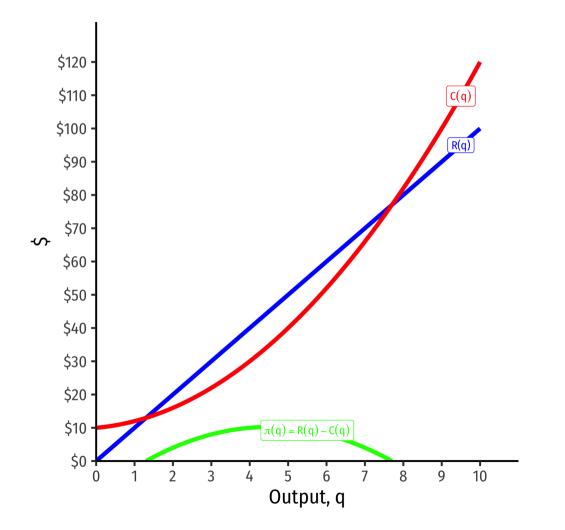


•  $\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$ 

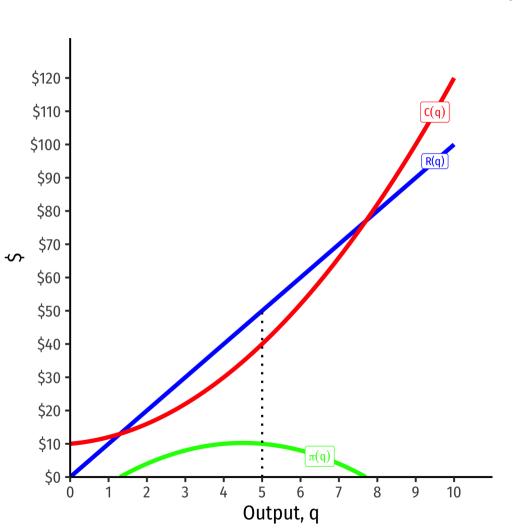


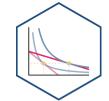


•  $\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$ 



- $\pi(q) = \mathbf{R}(q) \mathbf{C}(q)$
- Graph: find  $q^*$  to max  $\pi \implies q^*$ where max distance between R(q) and C(q)

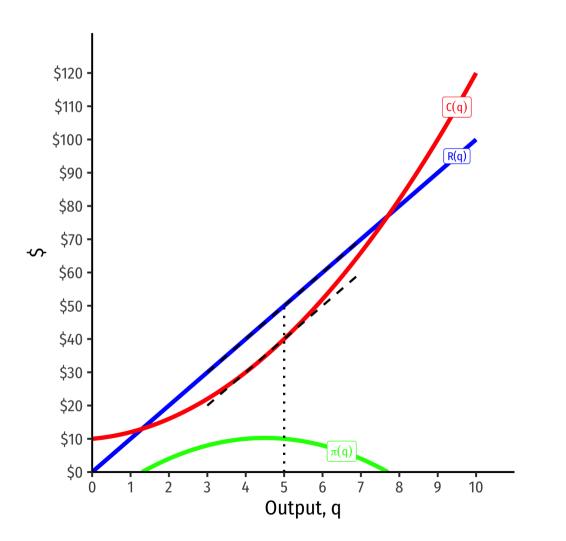


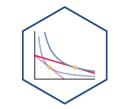


• 
$$\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$$

- Graph: find  $q^*$  to max  $\pi \implies q^*$ where max distance between R(q) and C(q)
- Slopes must be equal:

MR(q) = MC(q)



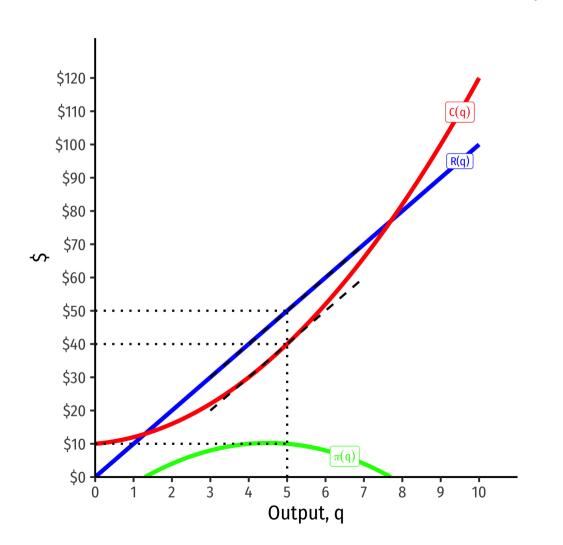


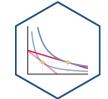
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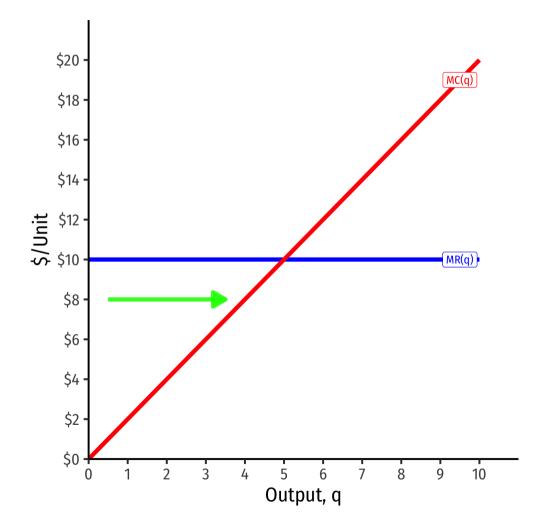
• At  $q^* = 5$ :  $\circ R(q) = 50$   $\circ C(q) = 40$  $\circ \pi(q) = 10$ 





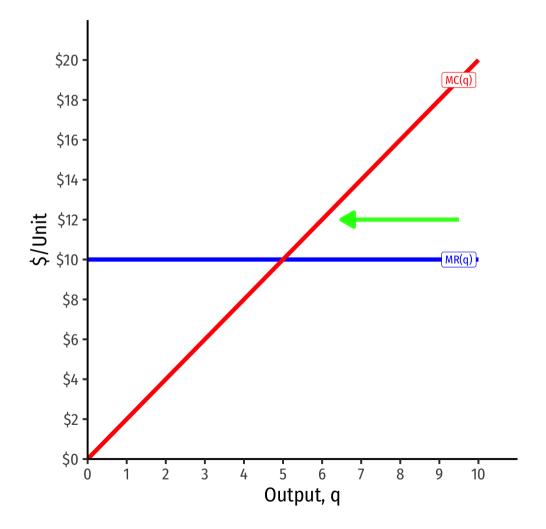
#### Visualizing Profit Per Unit As MR(q) and MC(q)

• At low output  $q < q^*$ , can increase  $\pi$  by producing *more*: MR(q) > MC(q)



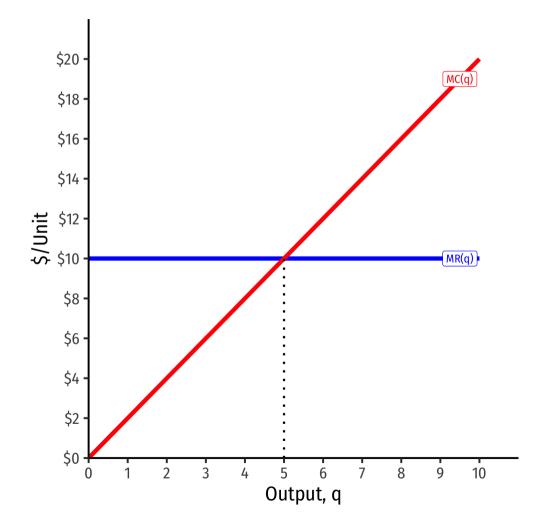
#### Visualizing Profit Per Unit As MR(q) and MC(q)

• At high output  $q > q^*$ , can increase  $\pi$ by producing *less*: MR(q) < MC(q)



#### Visualizing Profit Per Unit As MR(q) and MC(q)

•  $\pi$  is *maximized* where MR(q) = MC(q)

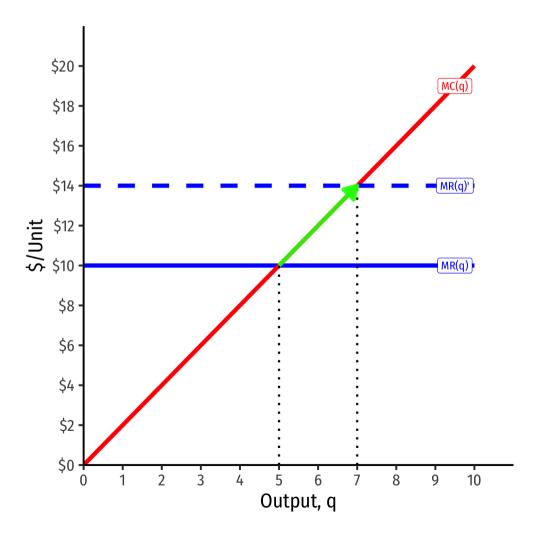


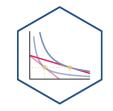


# **Comparative Statics**

#### **If Market Price Changes I**

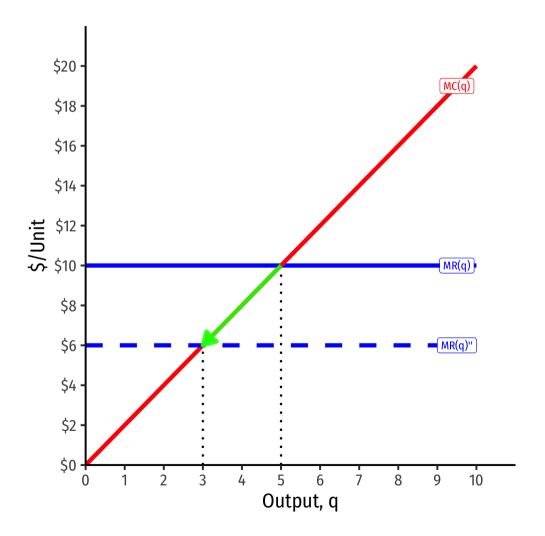
- Suppose the market price *increases*
- Firm (always setting MR = MC) will respond by *producing more*





#### **If Market Price Changes II**

- Suppose the market price *decreases*
- Firm (always setting MR = MC) will respond by *producing more*



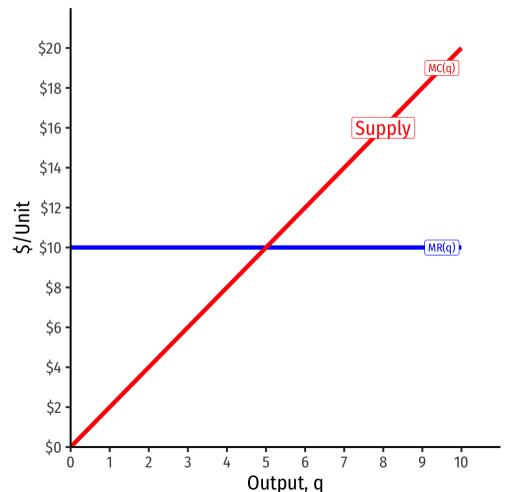
#### If Market Price Changes II

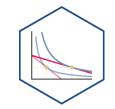
 The firm's marginal cost curve is its (inverse) supply curve<sup>†</sup>

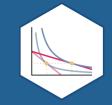
*Inv.* Supply(q) = MC(q)

 How it will supply the optimal amount of output in response to the market price

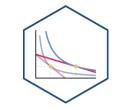






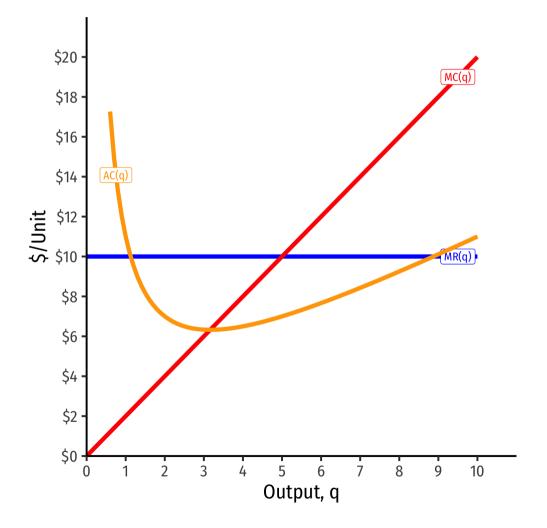


# **Calculating Profit**



• Profit is

$$\pi(q) = R(q) - C(q)$$

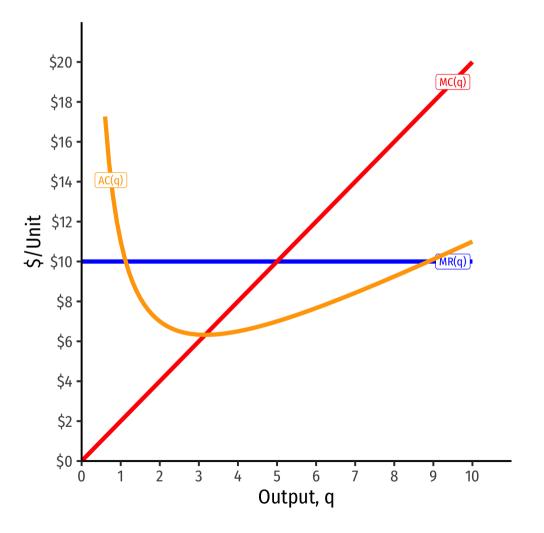


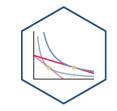


$$\pi(q) = R(q) - C(q)$$

• Profit per unit can be calculated as:

$$\frac{\pi(q)}{q} = AR(q) - AC(q)$$
$$= p - AC(q)$$





• Profit is

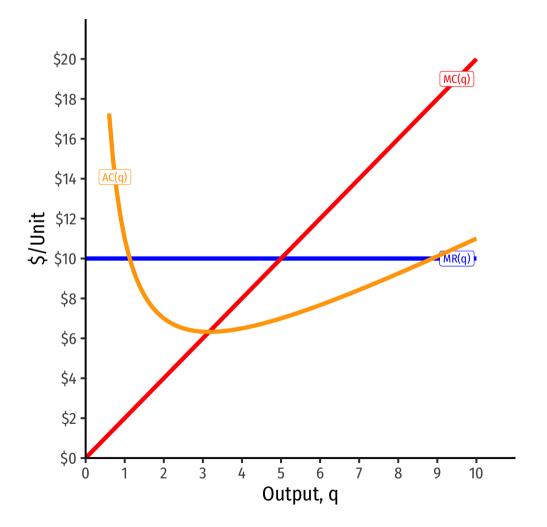
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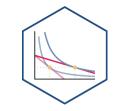
• Profit per unit can be calculated as:

$$\frac{\pi(q)}{q} = AR(q) - AC(q)$$
$$= p - AC(q)$$

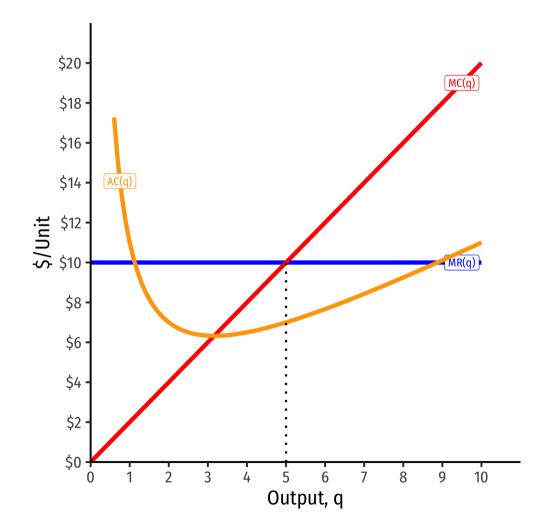
• Multiply by *q* to get total profit:

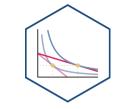
 $\pi(q) = q \left[ p - AC(q) \right]$ 





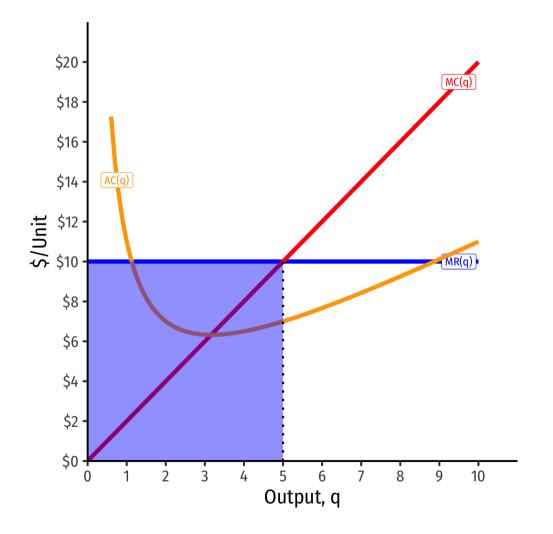
- At market price of p\* = \$10
- At q\* = 5 (per unit):
- At q\* = 5 (totals):





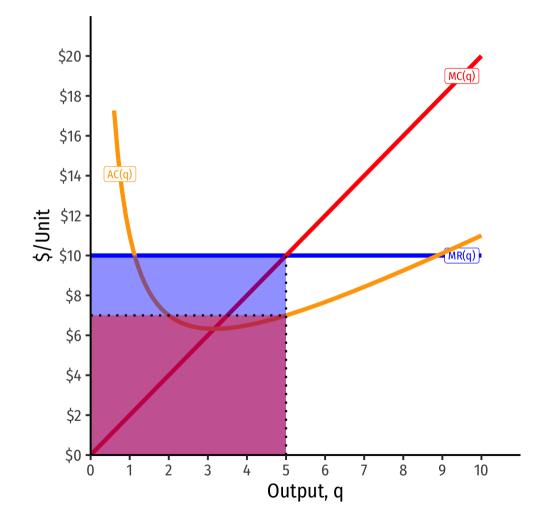
- At market price of p\* = \$10
- At q\* = 5 (per unit):
  - AR(5) = \$10/unit
- At q\* = 5 (totals):

• R(5) = \$50

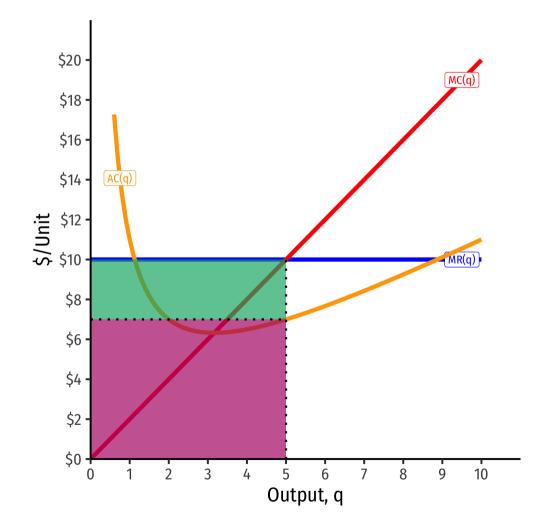


- At market price of p\* = \$10
- At q\* = 5 (per unit):
  - AR(5) = \$10/unit
    AC(5) = \$7/unit
- At q\* = 5 (totals):

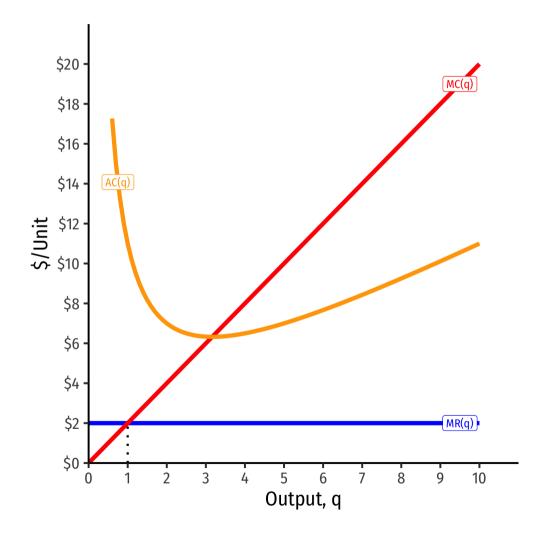
R(5) = \$50
C(5) = \$35

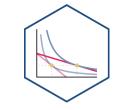


- At market price of p\* = \$10
- At q\* = 5 (per unit):
  - AR(5) = \$10/unit
  - AC(5) = \$7/unit
  - $A\pi(5) = \frac{3}{\text{unit}}$
- At q\* = 5 (totals):
  - R(5) = \$50
    C(5) = \$35



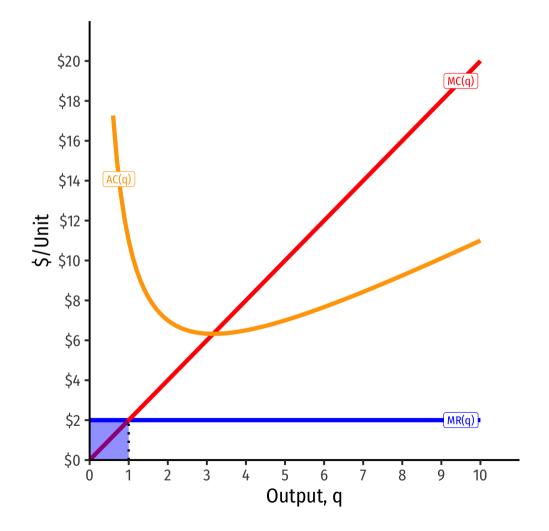
- At market price of p\* = \$2
- At q\* = 1 (per unit):
- At q\* = 1 (totals):





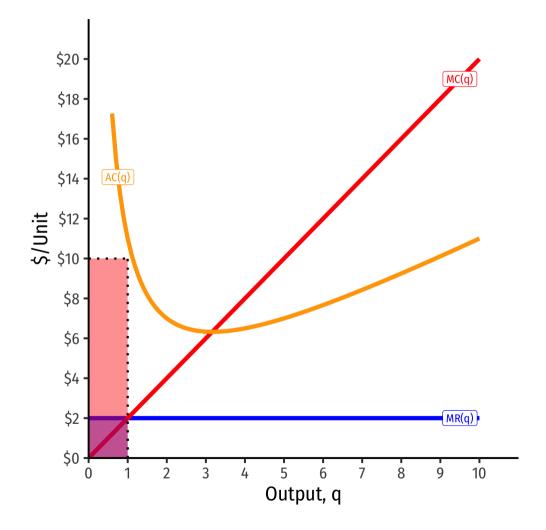
- At market price of p\* = \$2
- At q\* = 1 (per unit):
  - AR(1) = \$2/unit
- At q\* = 1 (totals):

• R(1) = \$2

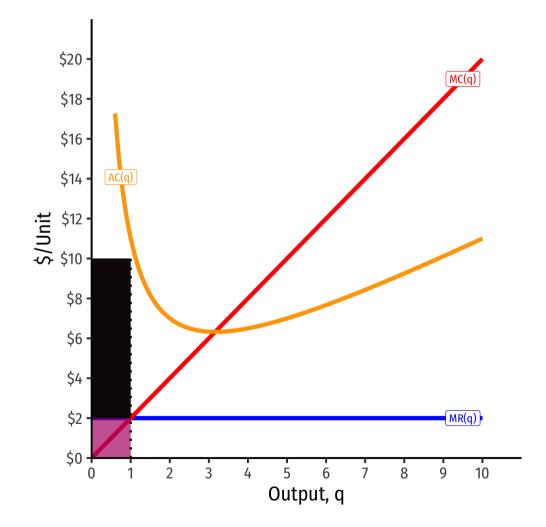


- At market price of p\* = \$2
- At q\* = 1 (per unit):
  - AR(1) = \$2/unit
    AC(1) = \$10/unit
- At q\* = 1 (totals):

R(1) = \$2
C(1) = \$10



- At market price of p\* = \$2
- At q\* = 1 (per unit):
  - AR(1) = \$2/unit
  - AC(1) = \$10/unit
  - $A\pi(1) = -\$8/unit$
- At q\* = 1 (totals):
  - R(1) = \$2
  - C(1) = \$10





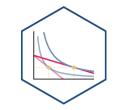
- What if a firm's profits at  $q^*$  are **negative** (i.e. it earns **losses**)?
- Should it produce at all?



- Suppose firm chooses to produce **nothing** (q = 0):
- If it has **fixed costs** (*f* > 0), its profits are:

$$\pi(q) = pq - C(q)$$

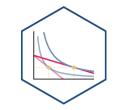




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- If it has **fixed costs** (*f* > 0), its profits are:

$$\begin{aligned} \pi(q) &= pq - C(q) \\ \pi(q) &= pq - f - VC(q) \end{aligned}$$

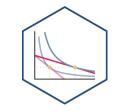




- Suppose firm chooses to produce **nothing** (q = 0):
- If it has **fixed costs** (*f* > 0), its profits are:

$$\begin{aligned} \pi(q) &= pq - C(q) \\ \pi(q) &= pq - f - VC(q) \\ \pi(0) &= -f \end{aligned}$$





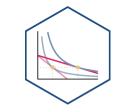
• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi$  from producing <  $\pi$  from not producing



• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi$  from producing <  $\pi$  from not producing  $\pi(q) < -f$ 



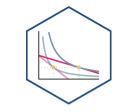
• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi$  from producing  $< \pi$  from not producing  $\pi(q) < -f$ pq - VC(q) - f < -f



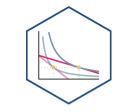
• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi \text{ from producing } < \pi \text{ from not producing}$  $\pi(q) < -f$ pq - VC(q) - f < -fpq - VC(q) < 0



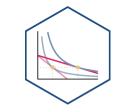
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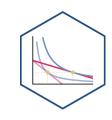


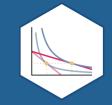
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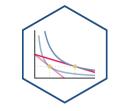
 $\pi \text{ from producing } < \pi \text{ from not producing}$   $\pi(q) < -f$  pq - VC(q) - f < -f pq - VC(q) < 0 pq < VC(q) p < AVC(q)

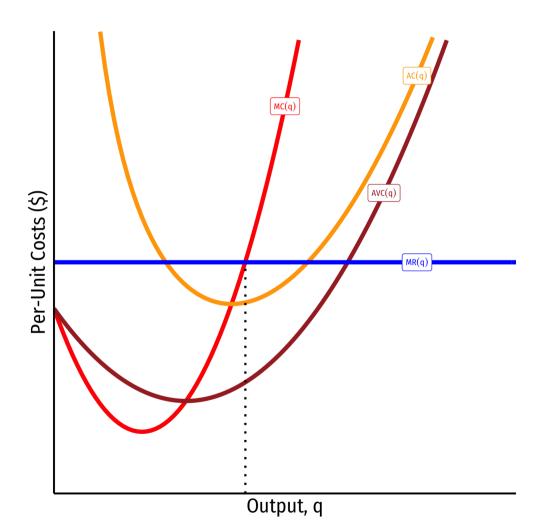


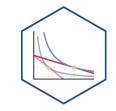
 Shut down price: firm will shut down production *in the short run* when p < AVC(q)</li>

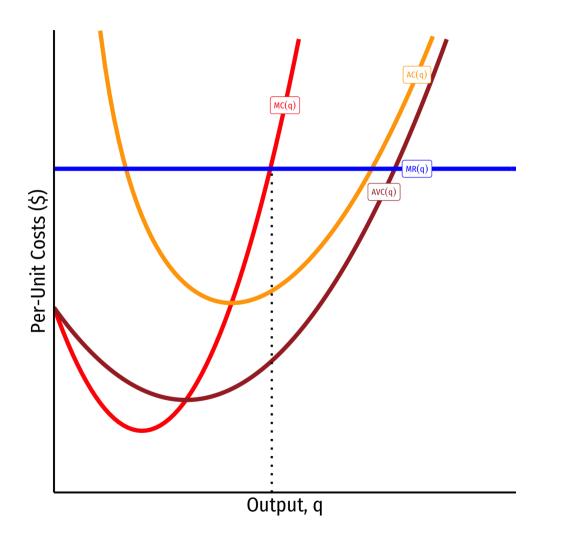


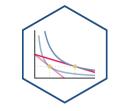


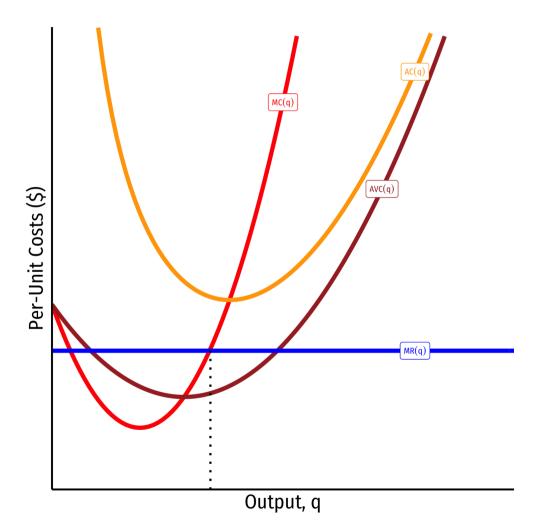


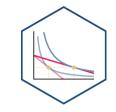


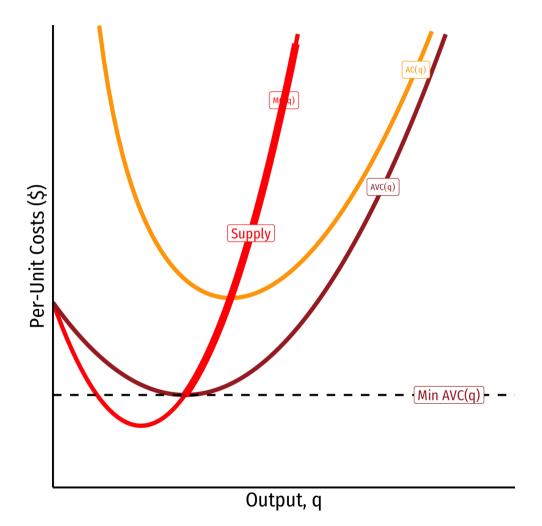


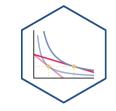


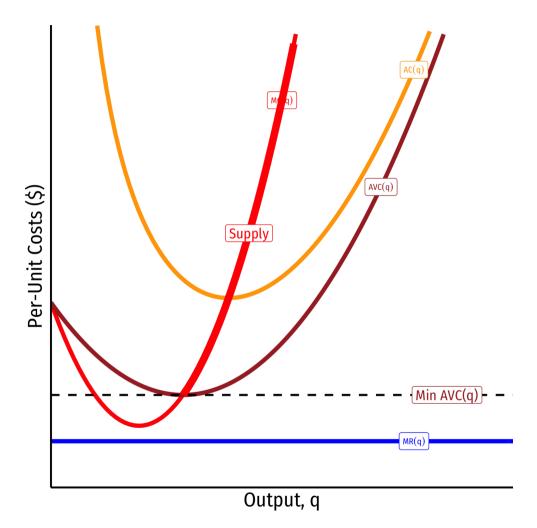


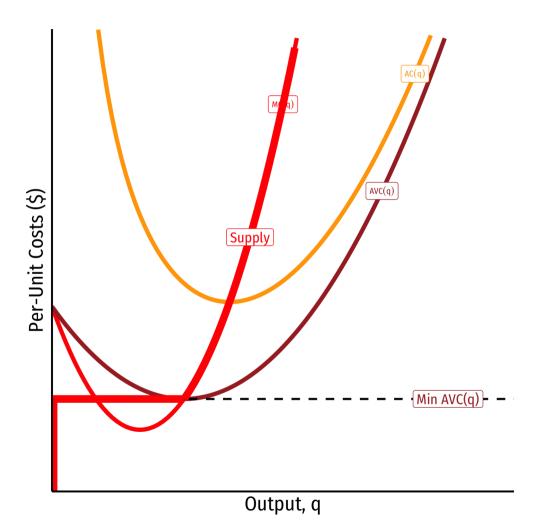






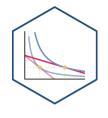


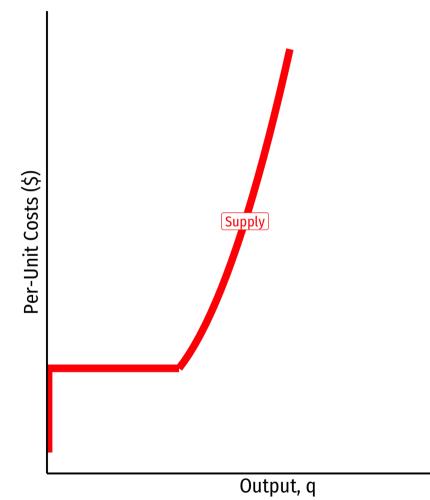




Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

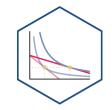




Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

#### **Summary:**



#### **1.** Choose $q^*$ such that MR(q) = MC(q)

- **2.** Profit  $\pi = q[p AC(q)]$
- 3. Shut down if p < AVC(q)

Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

# Choosing the Profit-Maximizing Output $q^*$ : Example

**Example**: Bob's barbershop gives haircuts in a very competitive market, where barbers cannot differentiate their haircuts. The current market price of a haircut is \$15. Bob's daily short run costs are given by:

$$C(q) = 0.5q^2$$
$$MC(q) = q$$

1. How many haircuts per day would maximize Bob's profits?

2. How much profit will Bob earn per day?

3. Find Bob's shut down price.