2.5 — Short Run Profit Maximization ECON 306 • Microeconomic Analysis • Fall 2021 Ryan Safner Assistant Professor of Economics ✓ safner@hood.edu

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Outline

Revenues

<u>Profits</u>

Comparative Statics

Calculating Profit

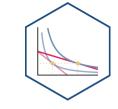
Short-Run Shut-Down Decisions

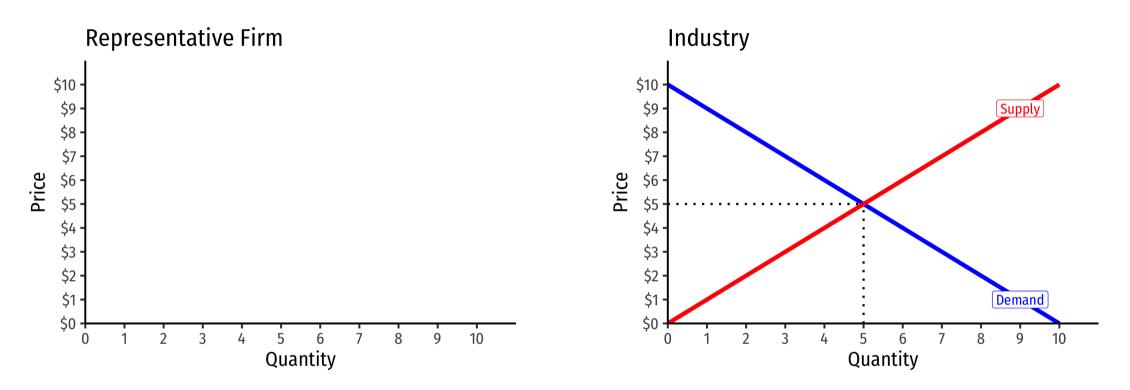
The Firm's Short-Run Supply Decision



Revenues

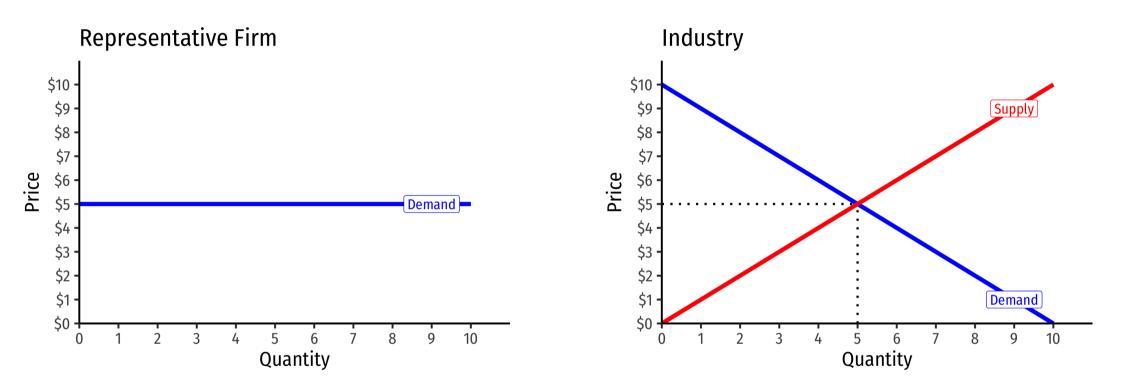
Revenues for Firms in *Competitive* **Industries I**





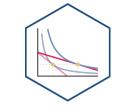
Revenues for Firms in *Competitive* **Industries I**

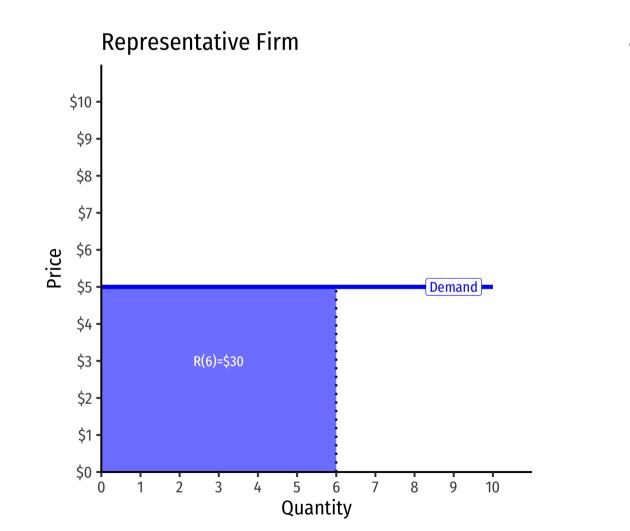




- Demand for a firm's product is **perfectly elastic** at the market price
- Where did the supply curve come from? You'll see

Revenues for Firms in Competitive Industries II





• Total Revenue R(q) = pq

Average and Marginal Revenues

• Average Revenue: revenue per unit of output

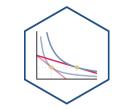
$$AR(q) = \frac{R}{q}$$

• AR(q) is **always** equal to the price! Why?

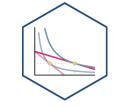
• Marginal Revenue: change in revenues for each additional unit of output sold:

$$MR(q) = \frac{\Delta R(q)}{\Delta q} \approx \frac{R_2 - R_1}{q_2 - q_1}$$

- Calculus: first derivative of the revenues function
- For a <u>competitive</u> firm (only), MR(q) = p, the price!



Average and Marginal Revenues: Example



Example: A firm sells bushels of wheat in a very competitive market. The current market price is \$10/bushel.

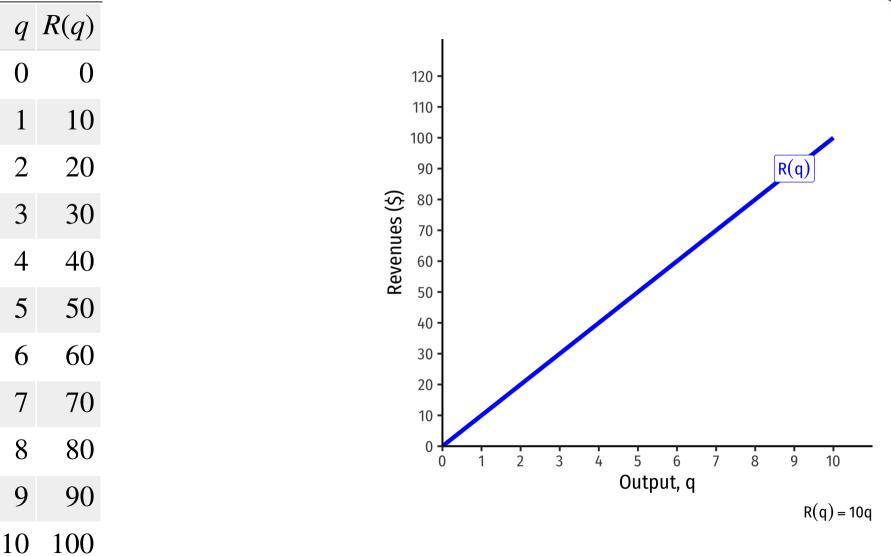
For the 1st bushel sold:

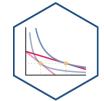
- What is the total revenue?
- What is the average revenue?

For the 2nd bushel sold:

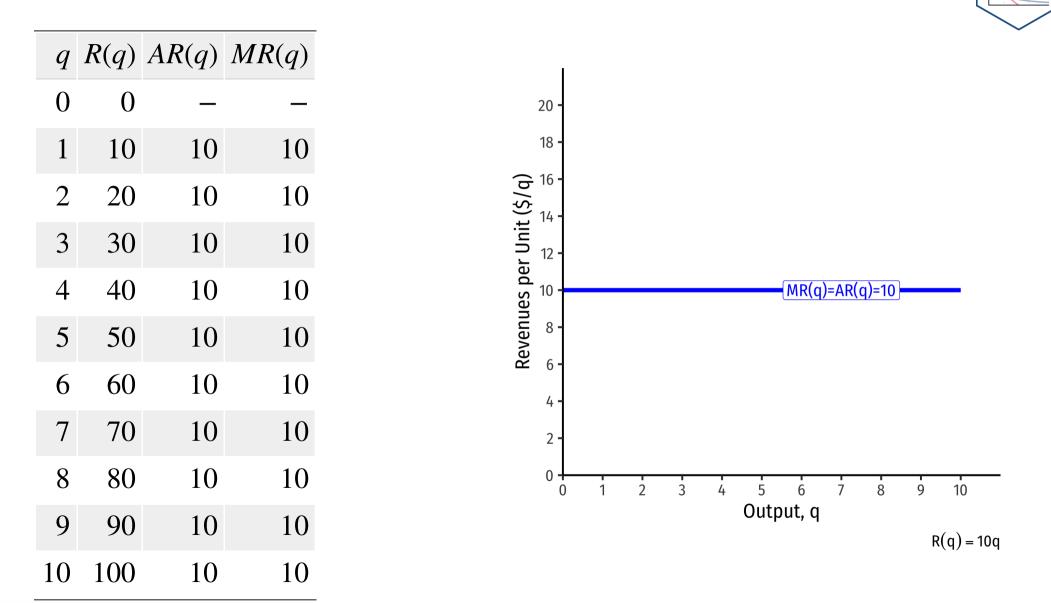
- What is the total revenue?
- What is the average revenue?
- What is the marginal revenue?

Total Revenue, Example: Visualized





Average and Marginal Revenue, Example: Visualized



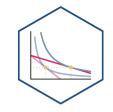


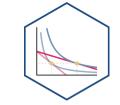
Profits

Recall: The Firm's Two Problems

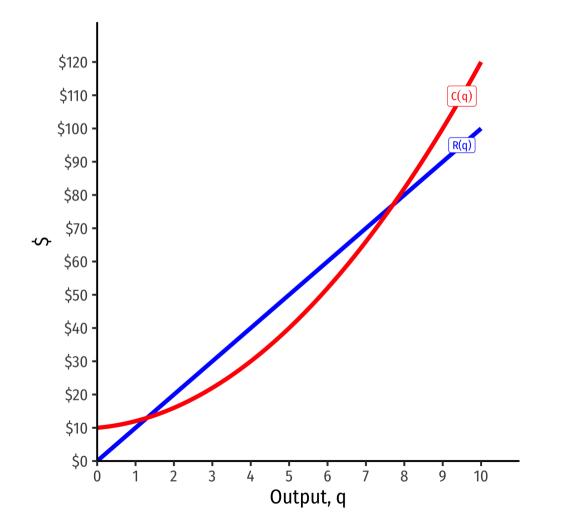
- 1st Stage: firm's profit maximization problem:
 - 1. Choose: < output >
 - 2. In order to maximize: < profits >
- 2nd Stage: firm's cost minimization problem:
 - 1. Choose: < inputs >
 - 2. In order to *minimize*: < cost >
 - 3. Subject to: < producing the optimal output >
 - Minimizing costs \iff maximizing profits

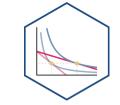




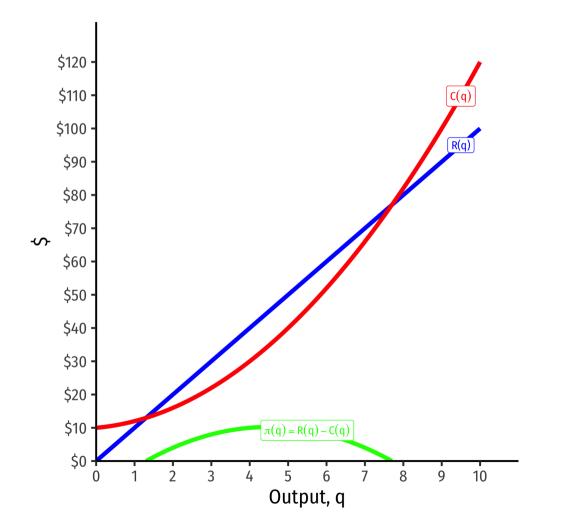


• $\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$

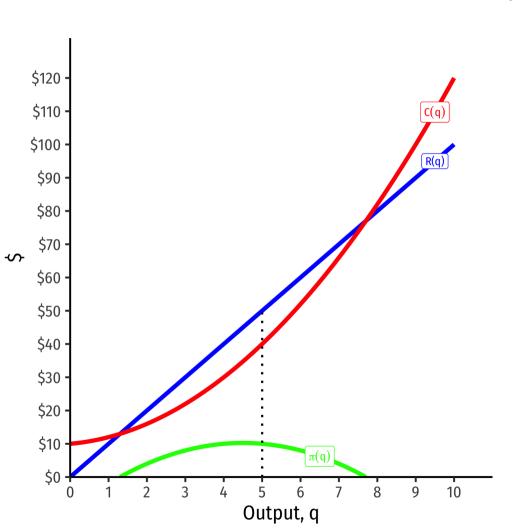


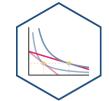


• $\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$



- $\pi(q) = \mathbf{R}(q) \mathbf{C}(q)$
- Graph: find q^* to max $\pi \implies q^*$ where max distance between R(q) and C(q)

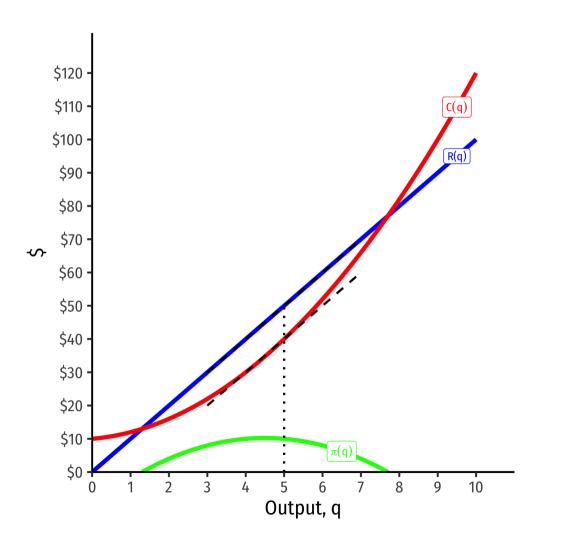


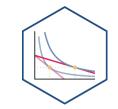


•
$$\pi(q) = \mathbf{R}(q) - \mathbf{C}(q)$$

- Graph: find q^* to max $\pi \implies q^*$ where max distance between R(q) and C(q)
- Slopes must be equal:

MR(q) = MC(q)



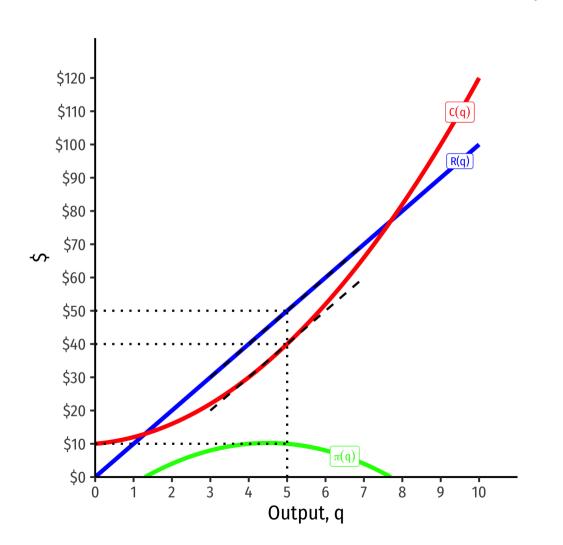


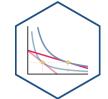
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- Graph: find q^* to max $\pi \implies q^*$ where max distance between R(q) and C(q)
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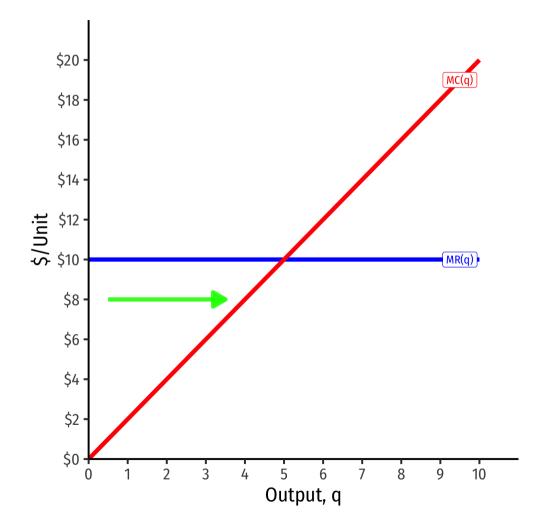
• At $q^* = 5$: $\circ R(q) = 50$ $\circ C(q) = 40$ $\circ \pi(q) = 10$





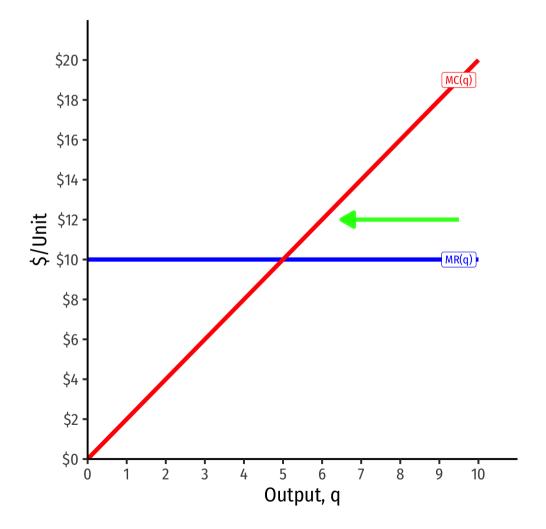
Visualizing Profit Per Unit As MR(q) and MC(q)

• At low output $q < q^*$, can increase π by producing *more*: MR(q) > MC(q)



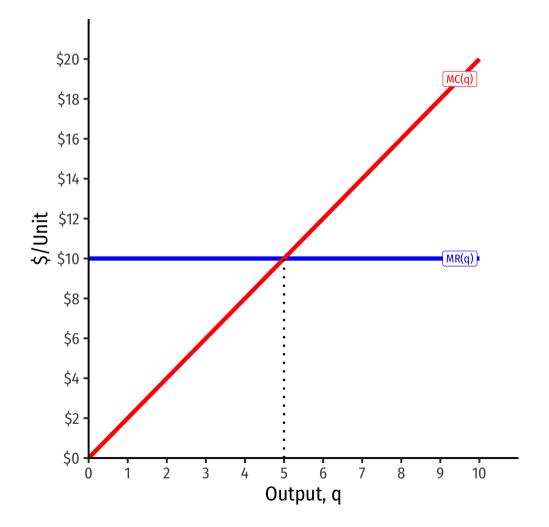
Visualizing Profit Per Unit As MR(q) and MC(q)

• At high output $q > q^*$, can increase π by producing *less*: MR(q) < MC(q)



Visualizing Profit Per Unit As MR(q) and MC(q)

• π is *maximized* where MR(q) = MC(q)

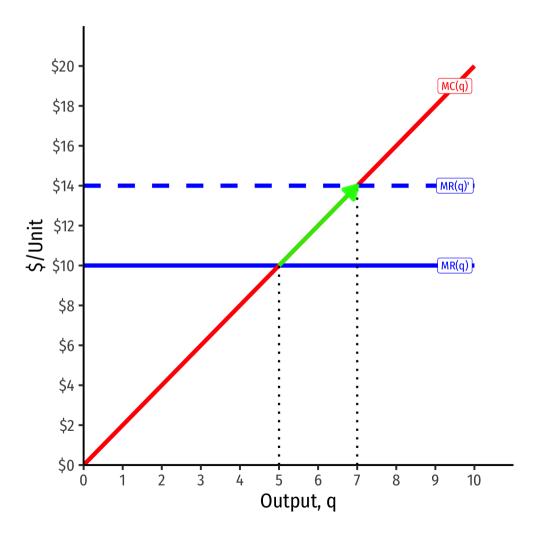


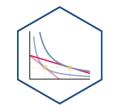


Comparative Statics

If Market Price Changes I

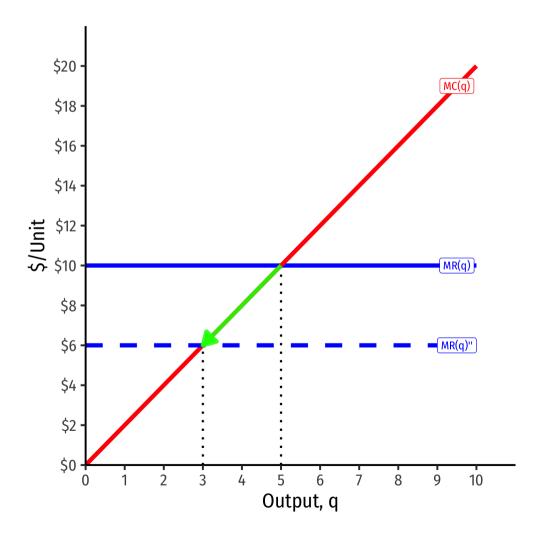
- Suppose the market price *increases*
- Firm (always setting MR = MC) will respond by *producing more*





If Market Price Changes II

- Suppose the market price *decreases*
- Firm (always setting MR = MC) will respond by *producing more*



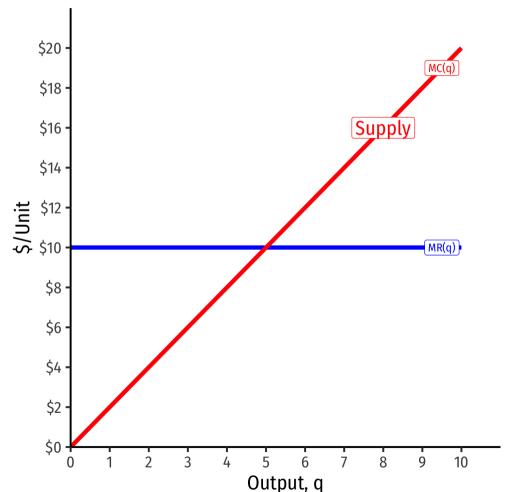
If Market Price Changes II

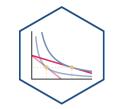
 The firm's marginal cost curve is its (inverse) supply curve[†]

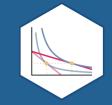
Inv. Supply(q) = MC(q)

 How it will supply the optimal amount of output in response to the market price

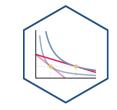






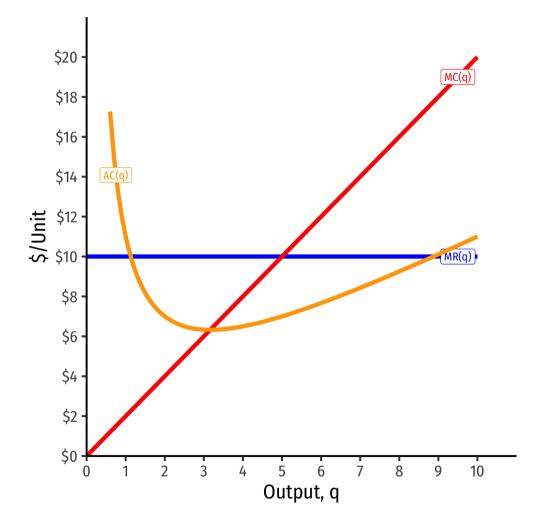


Calculating Profit



• Profit is

$$\pi(q) = R(q) - C(q)$$

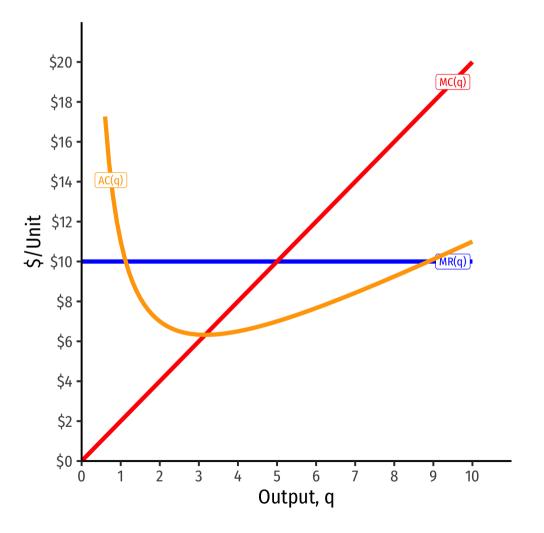


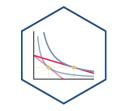


$$\pi(q) = R(q) - C(q)$$

• Profit per unit can be calculated as:

$$\frac{\pi(q)}{q} = AR(q) - AC(q)$$
$$= p - AC(q)$$





• Profit is

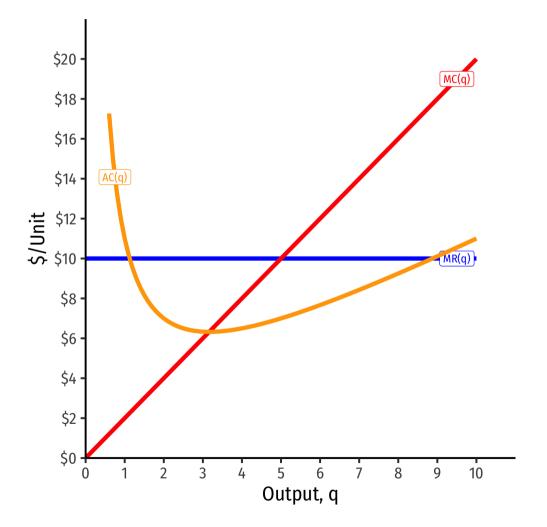
$$\pi(q) = R(q) - C(q)$$

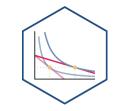
• Profit per unit can be calculated as:

$$\frac{\pi(q)}{q} = AR(q) - AC(q)$$
$$= p - AC(q)$$

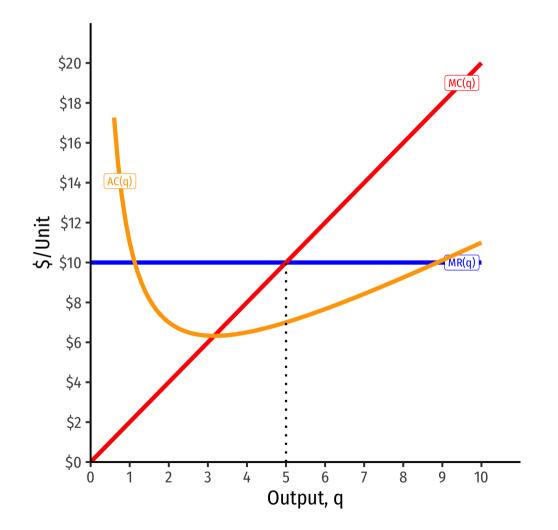
• Multiply by *q* to get total profit:

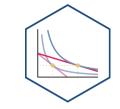
 $\pi(q) = q \left[p - AC(q) \right]$





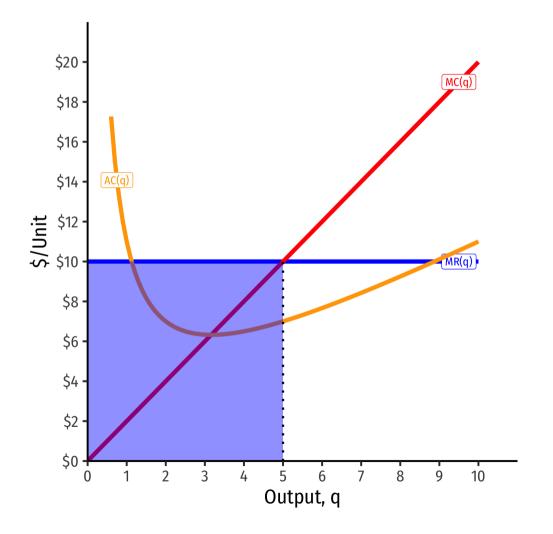
- At market price of p* = \$10
- At q* = 5 (per unit):
- At q* = 5 (totals):





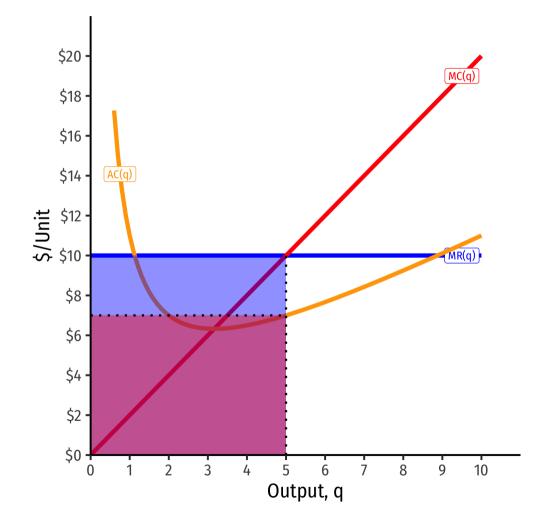
- At market price of p* = \$10
- At q* = 5 (per unit):
 - AR(5) = \$10/unit
- At q* = 5 (totals):

• R(5) = \$50

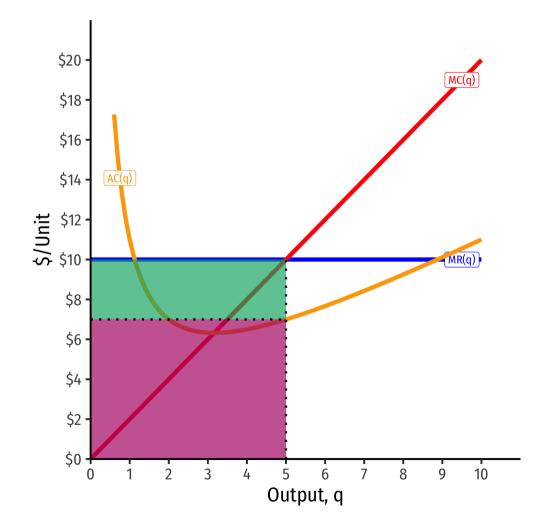


- At market price of p* = \$10
- At q* = 5 (per unit):
 - AR(5) = \$10/unit
 AC(5) = \$7/unit
- At q* = 5 (totals):

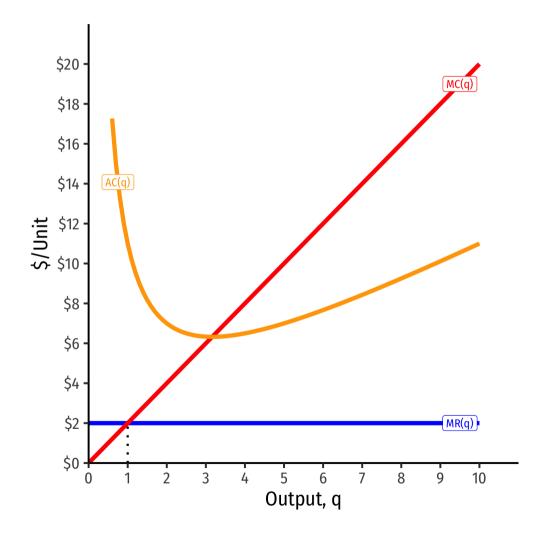
R(5) = \$50
C(5) = \$35

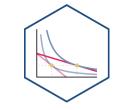


- At market price of p* = \$10
- At q* = 5 (per unit):
 - AR(5) = \$10/unit
 - AC(5) = \$7/unit
 - $A\pi(5) = \frac{3}{\text{unit}}$
- At q* = 5 (totals):
 - R(5) = \$50
 C(5) = \$35



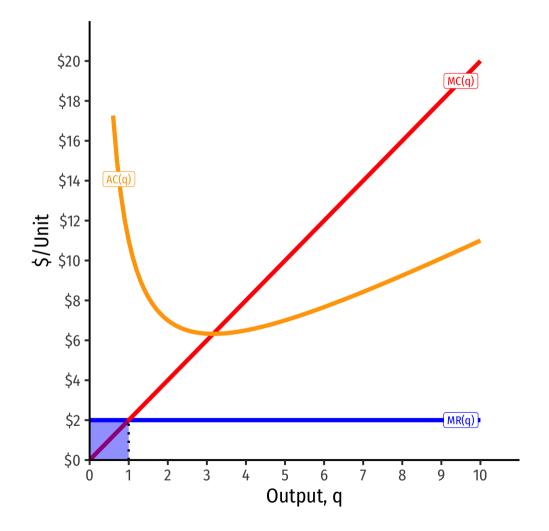
- At market price of p* = \$2
- At q* = 1 (per unit):
- At q* = 1 (totals):





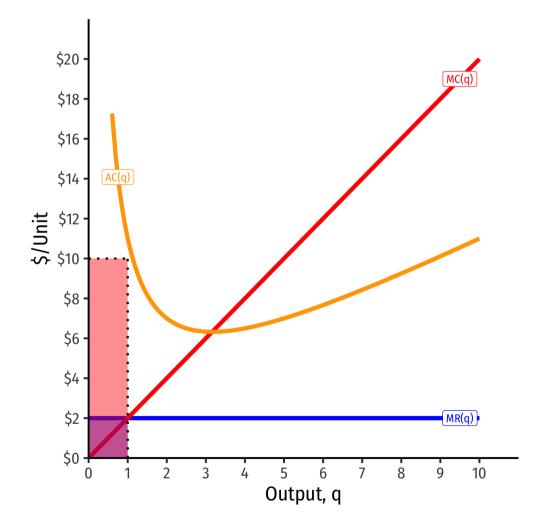
- At market price of p* = \$2
- At q* = 1 (per unit):
 - AR(1) = \$2/unit
- At q* = 1 (totals):

• R(1) = \$2

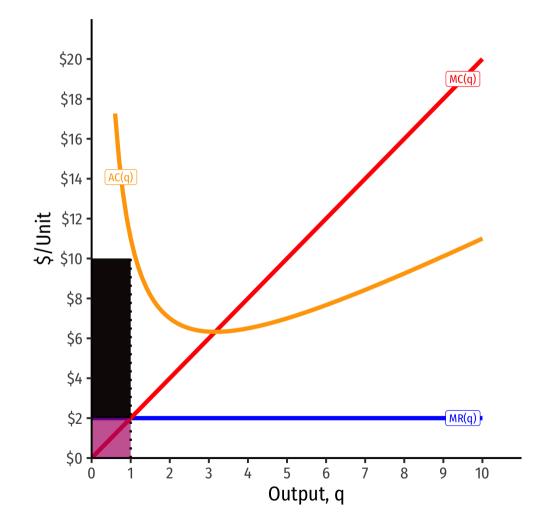


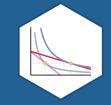
- At market price of p* = \$2
- At q* = 1 (per unit):
 - AR(1) = \$2/unit
 AC(1) = \$10/unit
- At q* = 1 (totals):

R(1) = \$2
C(1) = \$10



- At market price of p* = \$2
- At q* = 1 (per unit):
 - AR(1) = \$2/unit
 - AC(1) = \$10/unit
 - $A\pi(1) = -\$8/unit$
- At q* = 1 (totals):
 - R(1) = \$2
 - C(1) = \$10





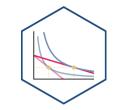
- What if a firm's profits at q^* are **negative** (i.e. it earns **losses**)?
- Should it produce at all?



- Suppose firm chooses to produce **nothing** (q = 0):
- If it has **fixed costs** (*f* > 0), its profits are:

$$\pi(q) = pq - C(q)$$

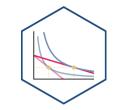




- Suppose firm chooses to produce **nothing** (q = 0):
- If it has **fixed costs** (*f* > 0), its profits are:

$$\begin{aligned} \pi(q) &= pq - C(q) \\ \pi(q) &= pq - f - VC(q) \end{aligned}$$

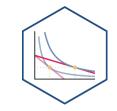




- Suppose firm chooses to produce **nothing** (q = 0):
- If it has **fixed costs** (*f* > 0), its profits are:

$$\begin{aligned} \pi(q) &= pq - C(q) \\ \pi(q) &= pq - f - VC(q) \\ \pi(0) &= -f \end{aligned}$$





• A firm should choose to produce **nothing** (q = 0) only when:

 π from producing < π from not producing



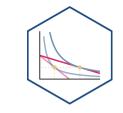
• A firm should choose to produce **nothing** (q = 0) only when:

 π from producing < π from not producing $\pi(q) < -f$



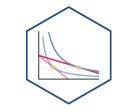
• A firm should choose to produce **nothing** (q = 0) only when:

 π from producing $< \pi$ from not producing $\pi(q) < -f$ pq - VC(q) - f < -f



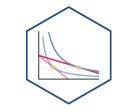
• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi \text{ from producing } < \pi \text{ from not producing}$ $\pi(q) < -f$ pq - VC(q) - f < -fpq - VC(q) < 0



• A firm should choose to produce **nothing** (q = 0) only when:

 $\pi \text{ from producing } < \pi \text{ from not producing}$ $\pi(q) < -f$ pq - VC(q) - f < -f pq - VC(q) < 0 pq < VC(q)

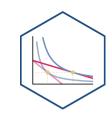


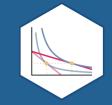
• A firm should choose to produce **nothing** (q = 0) only when:

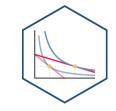
 $\pi \text{ from producing } < \pi \text{ from not producing}$ $\pi(q) < -f$ pq - VC(q) - f < -f pq - VC(q) < 0 pq < VC(q) p < AVC(q)

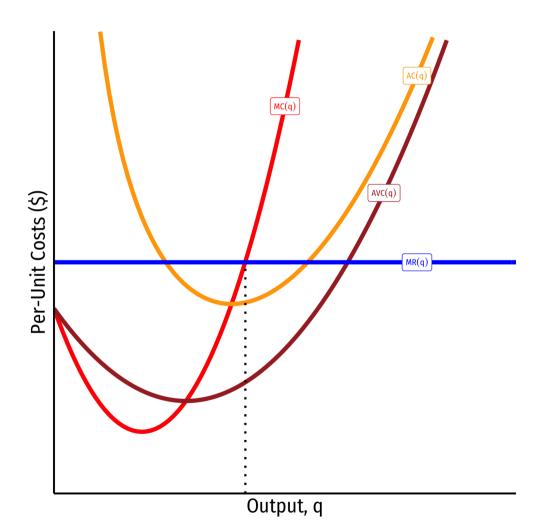


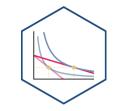
 Shut down price: firm will shut down production *in the short run* when p < AVC(q)

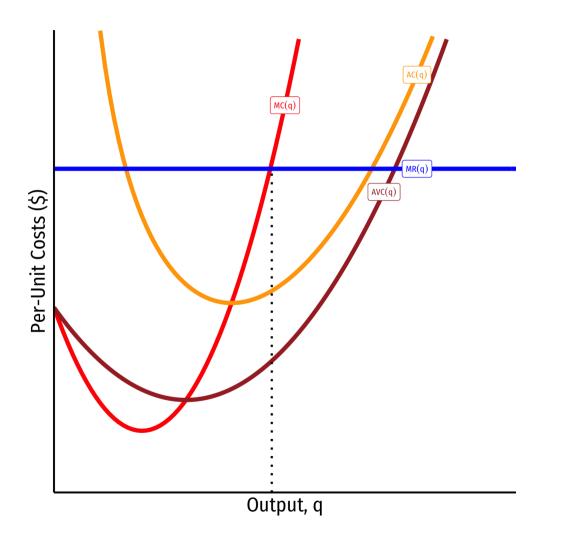


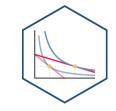


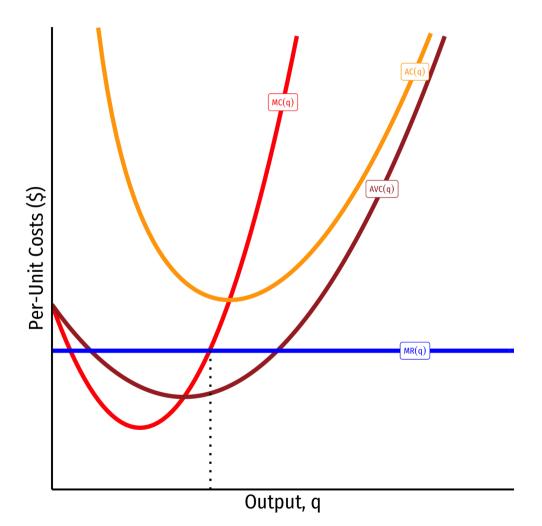


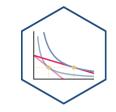


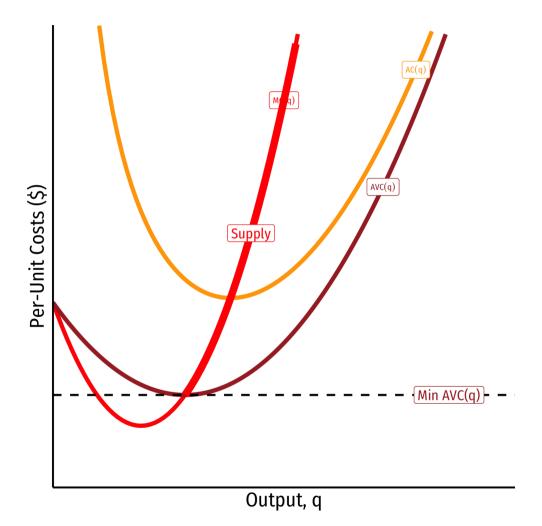


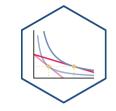


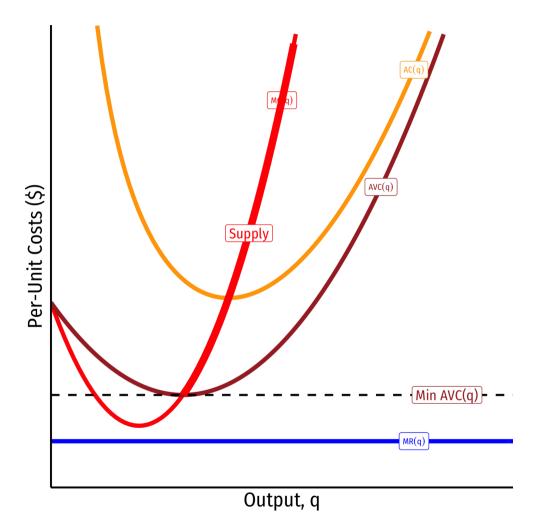


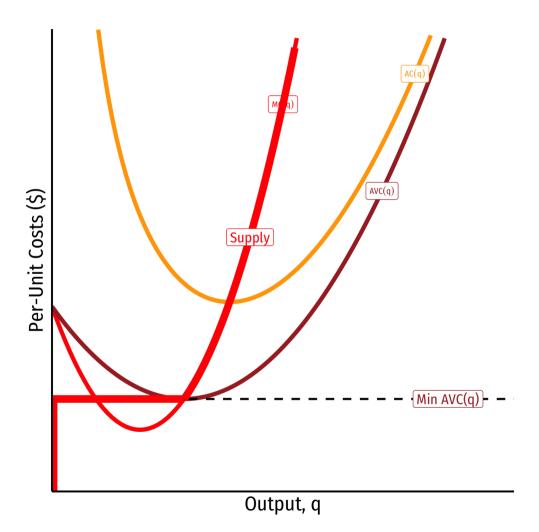






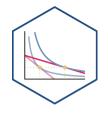


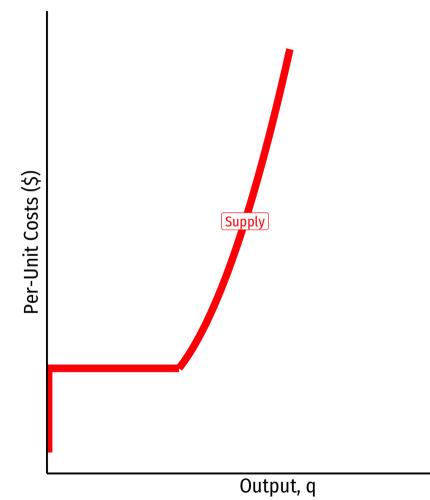




Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

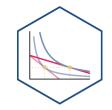




Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

Summary:



1. Choose q^* such that MR(q) = MC(q)

- **2.** Profit $\pi = q[p AC(q)]$
- 3. Shut down if p < AVC(q)

Firm's short run (inverse) supply:

$$\begin{cases} p = MC(q) & \text{if } p \ge AVC \\ q = 0 & \text{If } p < AVC \end{cases}$$

Choosing the Profit-Maximizing Output q^* : Example

Example: Bob's barbershop gives haircuts in a very competitive market, where barbers cannot differentiate their haircuts. The current market price of a haircut is \$15. Bob's daily short run costs are given by:

$$C(q) = 0.5q^2$$
$$MC(q) = q$$

1. How many haircuts per day would maximize Bob's profits?

2. How much profit will Bob earn per day?

3. Find Bob's shut down price.